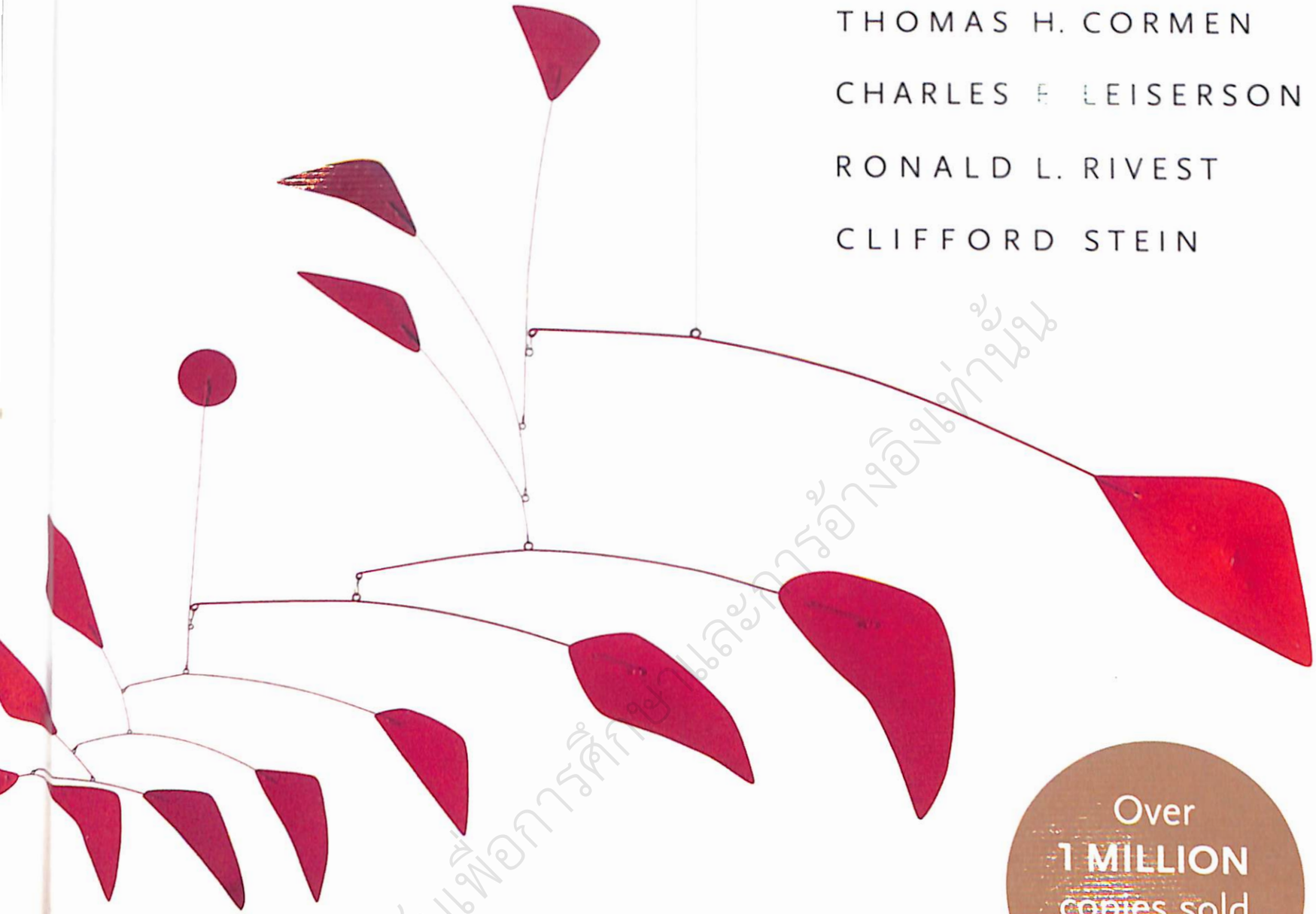
THOMAS H. CORMEN
CHARLES E. LEISERSON
RONALD L. RIVEST
CLIFFORD STEIN



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# INTRODUCTION TO ALGORITHMS

FOURTH EDITION

สำหรับเพื่อการศึกษาและการอ้างอิงเท่านั้น

มหาวิทยาลัยเทคโนโลยีราชมงคลพระนคร
ห้องสมุดสาขาพระนครเหนือ
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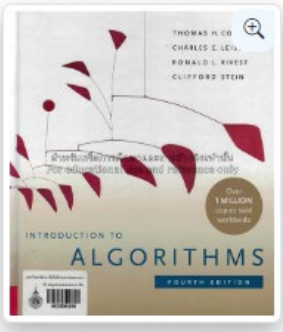


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